

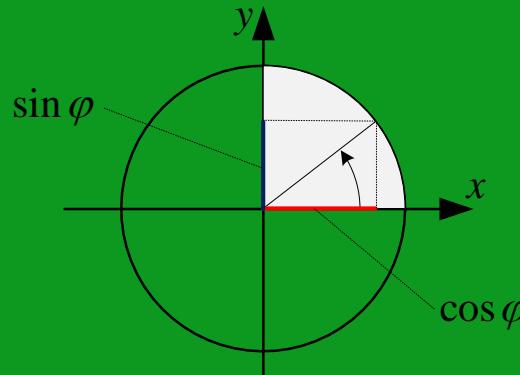


Smart Inverters

ФАКУЛТЕТ ТЕХНИЧКИХ НАУКА
САША ШТАТКИЋ



Producer Reference Frame (PRF) conventions power factor sign – quadrant I



$$\underline{U} = U e^{j\varphi}$$

$0 < \varphi < 90^\circ$

$$\underline{I} = I e^{j\psi} = I e^{j0^\circ} = I \cos 0^\circ + j I \sin 0^\circ = I$$

$$\underline{S} = \underline{U} \cdot \underline{I}^* = U e^{j\varphi} \cdot (I e^{j0})^* = U I e^{j\varphi} =$$

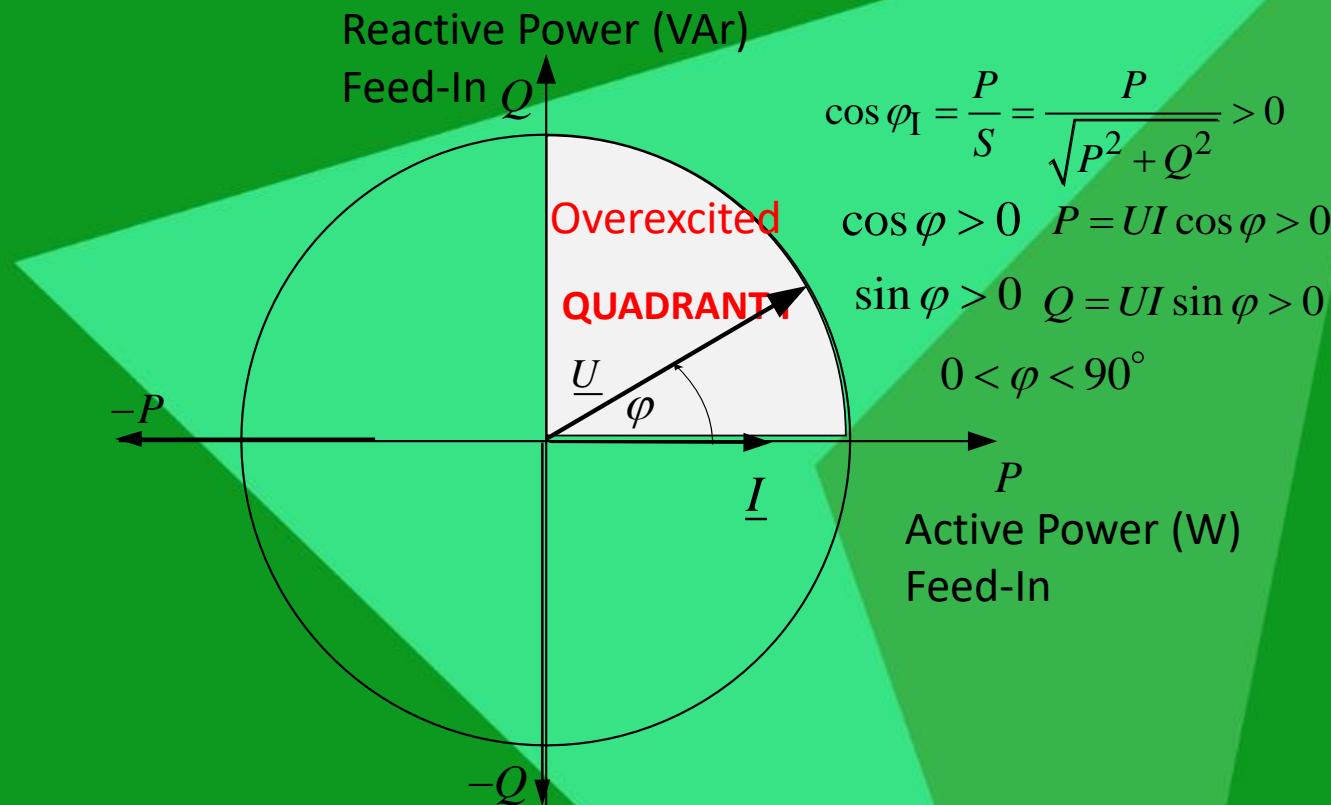
$$= U I (\cos \varphi + j \sin \varphi) = U I \cos \varphi + j U I \sin \varphi = P + j Q$$

$$\cos \varphi > 0$$

$$P = U I \cos \varphi > 0$$

$$\sin \varphi > 0$$

$$Q = U I \sin \varphi > 0$$



$$\cos \varphi_I = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} > 0$$

$$\cos \varphi > 0 \quad P = U I \cos \varphi > 0$$

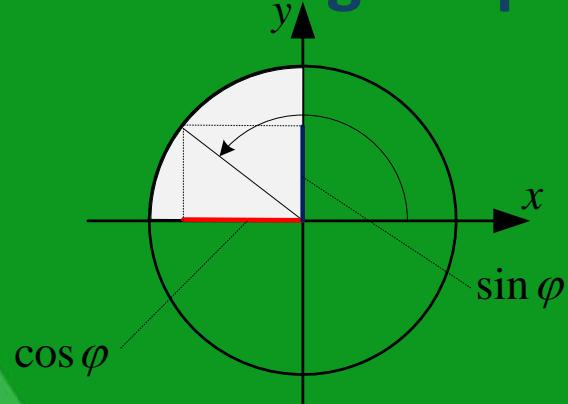
$$\sin \varphi > 0 \quad Q = U I \sin \varphi > 0$$

$$0 < \varphi < 90^\circ$$

Active Power (W)
Feed-In



Producer Reference Frame (PRF) conventions power factor sign – quadrant II



$$\underline{I} = I e^{j\psi} = I e^{j0^\circ} = I \cos 0^\circ + j I \sin 0^\circ = I$$

$$\underline{U} = U e^{j\phi} \quad 90^\circ < \phi < 180^\circ$$

$$\underline{S} = \underline{U} \cdot \underline{I}^* = U e^{j\phi} \cdot (I e^{j0})^* = U I e^{j\phi} = U I (\cos \phi + j \sin \phi) = U I \cos \phi + j U I \sin \phi = P + j Q$$

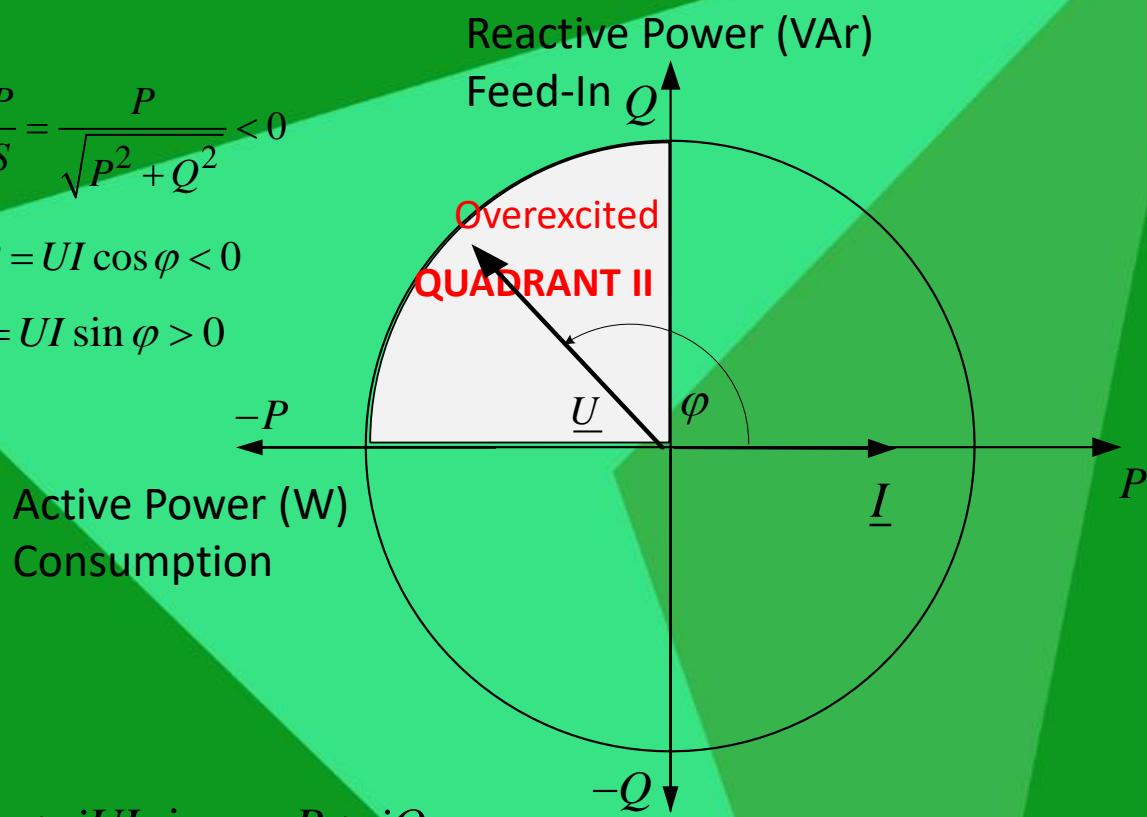
$$\begin{aligned} \cos \phi &< 0 & P &= U I \cos \phi < 0 \\ \sin \phi &> 0 & Q &= U I \sin \phi > 0 \end{aligned}$$

$$\cos \varphi_{II} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} < 0$$

$$\cos \varphi < 0 \quad P = U I \cos \varphi < 0$$

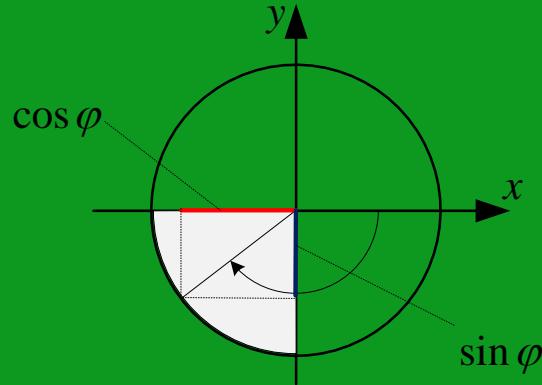
$$\sin \varphi > 0 \quad Q = U I \sin \varphi > 0$$

$$90^\circ < \varphi < 180^\circ$$





Producer Reference Frame (PRF) conventions power factor sign – quadrant III



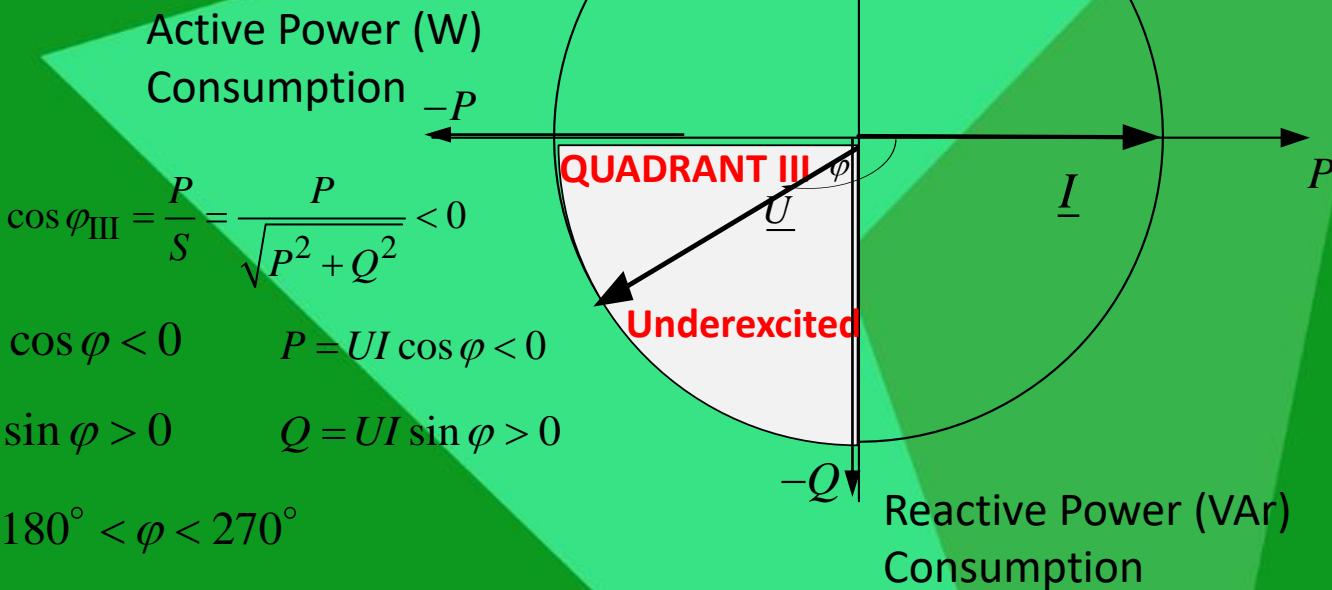
$$\underline{I} = I e^{j\psi} = I e^{j0^\circ} = I \cos 0^\circ + j I \sin 0^\circ = I$$

$$\underline{U} = U e^{j\varphi} \quad 180^\circ < \varphi < 270^\circ$$

$$\begin{aligned} \underline{S} &= \underline{U} \cdot \underline{I}^* = U e^{j\varphi} \cdot (I e^{j0})^* = U I e^{j\varphi} = \\ &= U I (\cos \varphi + j \sin \varphi) = U I \cos \varphi + j U I \sin \varphi = P + j Q \end{aligned}$$

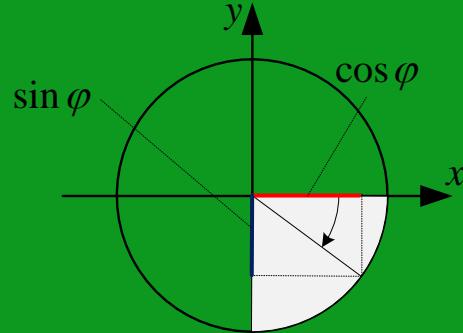
$$\cos \varphi < 0 \quad P = U I \cos \varphi < 0$$

$$\sin \varphi > 0 \quad Q = U I \sin \varphi > 0$$





Producer Reference Frame (PRF) conventions power factor sign – quadrant IV



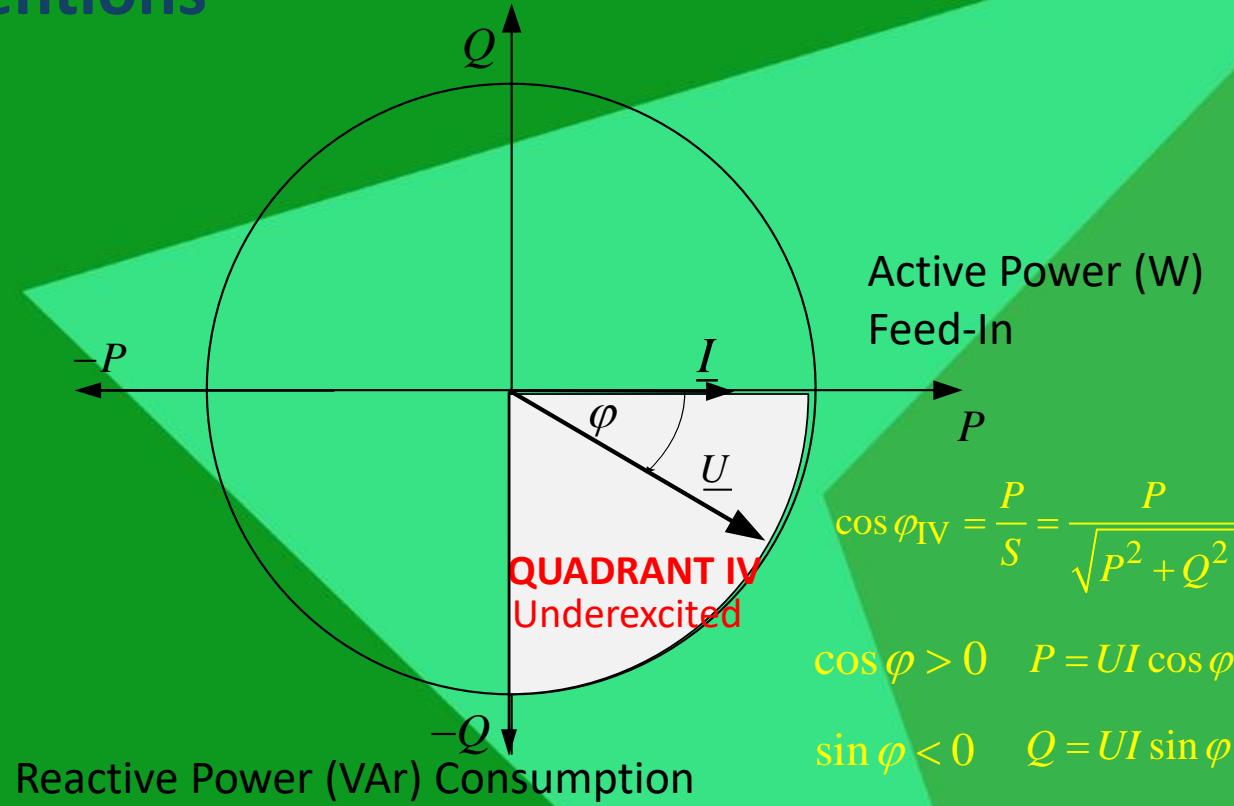
$$\underline{I} = I e^{j\psi} = I e^{j0^\circ} = I \cos 0^\circ + j I \sin 0^\circ = I$$

$$\underline{U} = U e^{j\varphi} \quad 270^\circ < \varphi < 360^\circ$$

$$\begin{aligned} \underline{S} &= \underline{U} \cdot \underline{I}^* = U e^{j\varphi} \cdot (I e^{j0^\circ})^* = U I e^{j\varphi} = \\ &= U I (\cos \varphi + j \sin \varphi) = U I \cos \varphi + j U I \sin \varphi = P + j Q \end{aligned}$$

$$\cos \varphi > 0 \quad P = U I \cos \varphi > 0$$

$$\sin \varphi < 0 \quad Q = U I \sin \varphi < 0$$



$$\cos \varphi_{IV} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} > 0$$

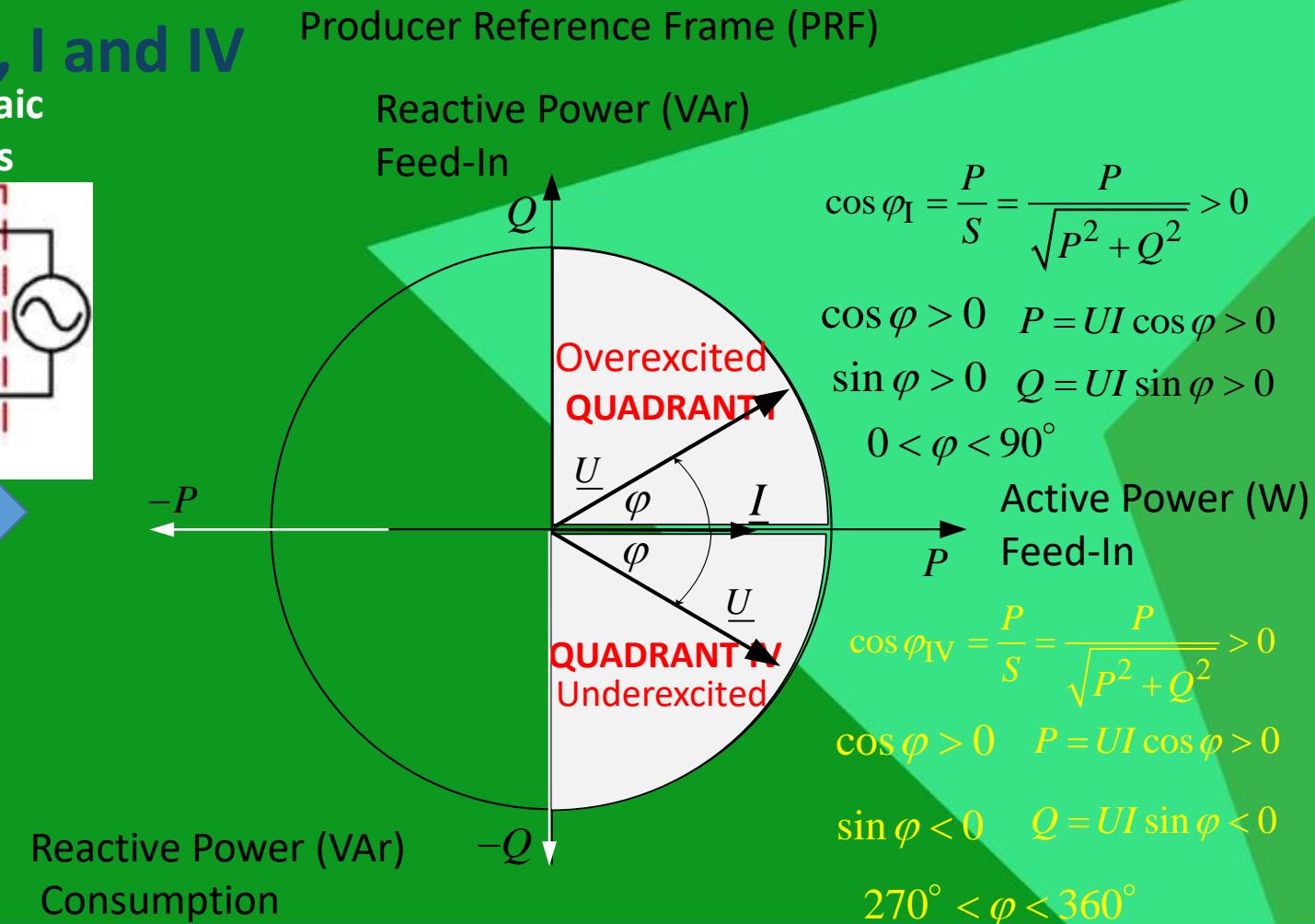
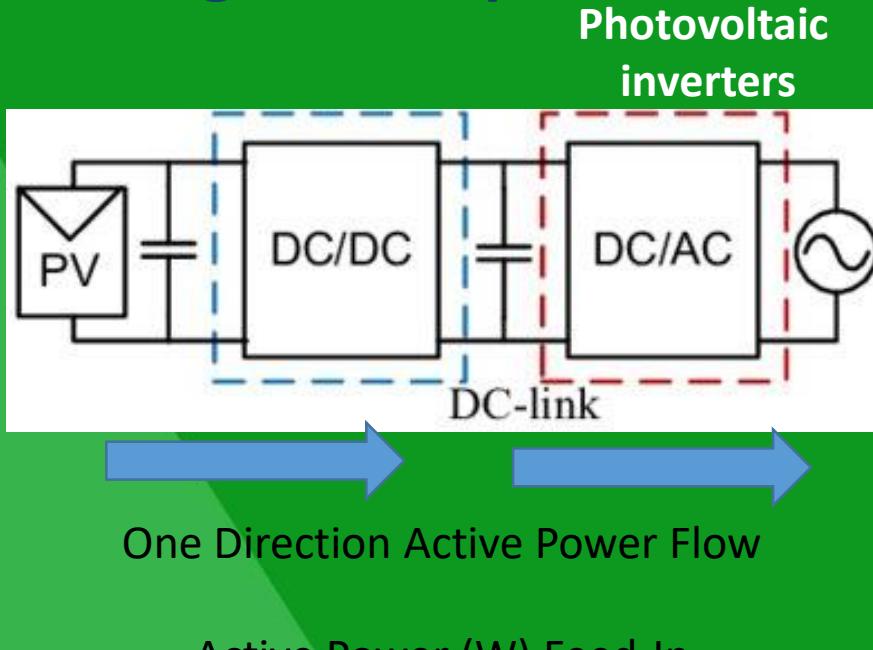
$$\cos \varphi > 0 \quad P = U I \cos \varphi > 0$$

$$\sin \varphi < 0 \quad Q = U I \sin \varphi < 0$$

$$270^\circ < \varphi < 360^\circ$$



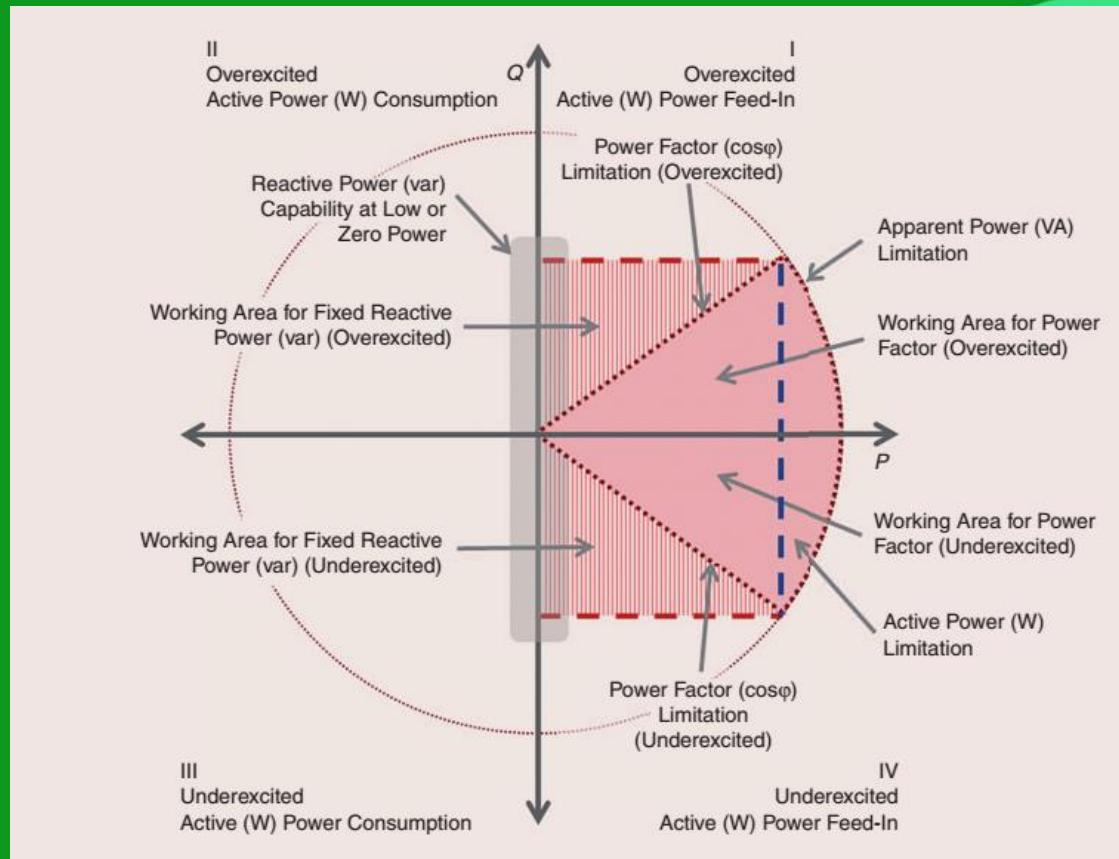
Photovoltaic inverters working area 2 quadrants, I and IV





A P-Q diagram of an inverter in Producer Reference Frame (PRF)

A P-Q diagram of an inverter, showing the device's working areas in terms of active and reactive power and different control modes, in the producer reference frame (PRF)



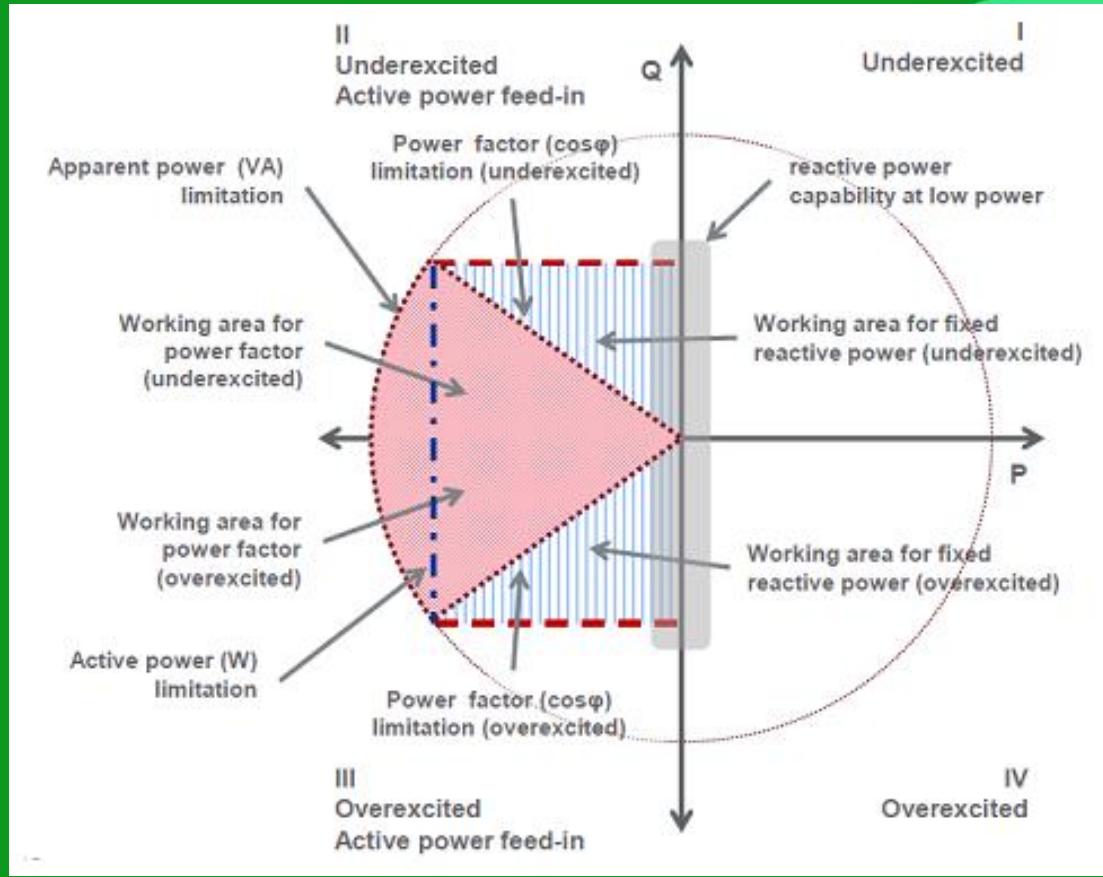
Producer Reference Frame (PRF)





A P-Q diagram of an inverter in Consumer Reference Frame (CRF)

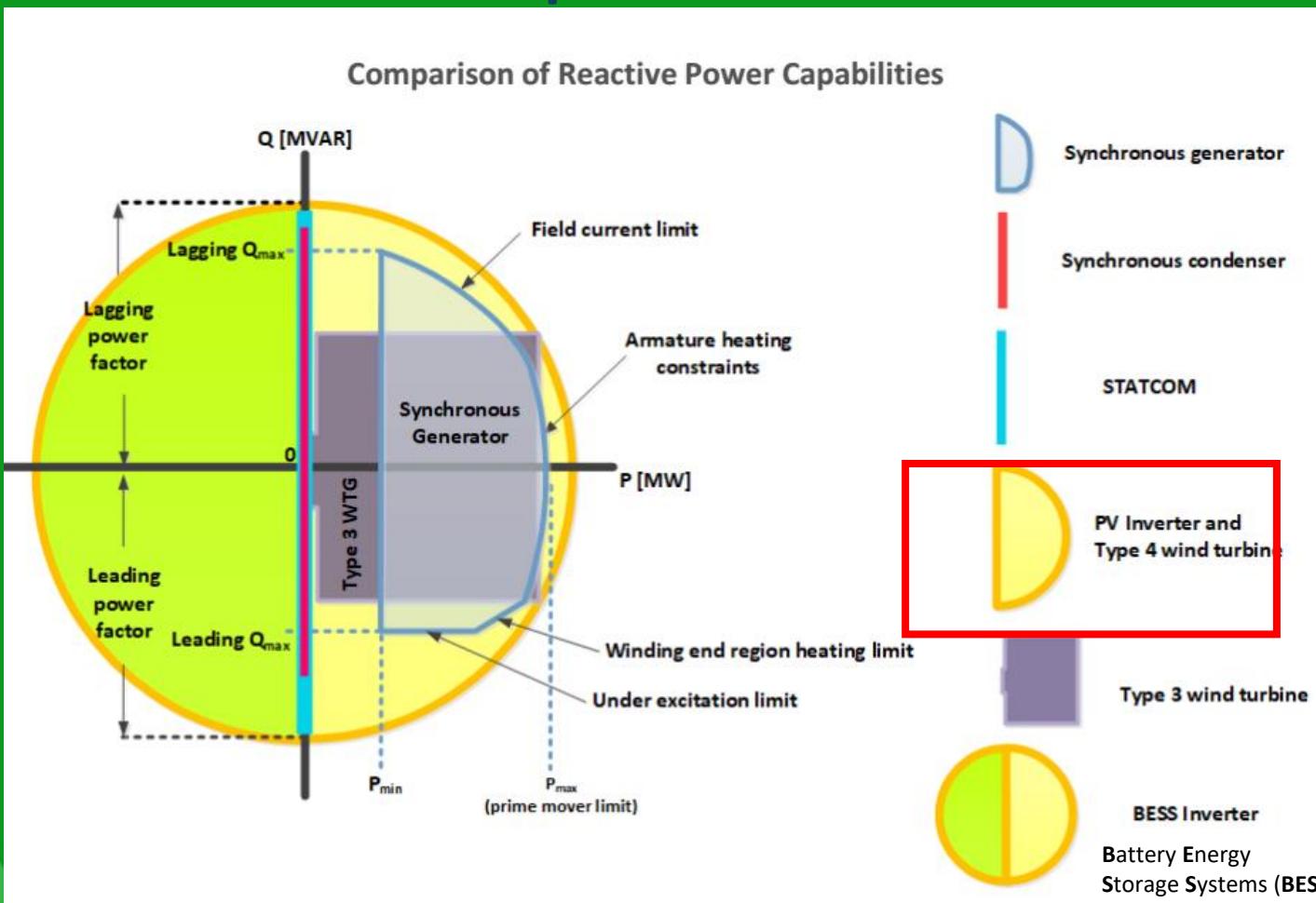
A P-Q diagram of an inverter, showing the device's working areas in terms of active and reactive power and different control modes, in the consumer reference frame (CRF)



Consumer Reference Frame (CRF)



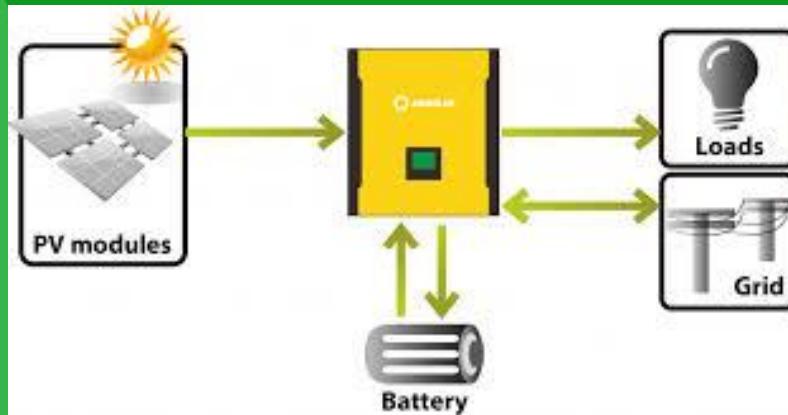
Comparison of Reactive Power Capabilities





Battery storage system inverters working area 4 quadrants, I, II, III and IV

Hybrid Photovoltaic Inverter



Bi-Direction Active Power Flow

Active Power (W) Feed-In

Active Power (W) Consumption

$$\cos \varphi_{\text{II}} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} < 0$$

$$\cos \varphi < 0 \quad P = UI \cos \varphi < 0$$

$$\sin \varphi > 0 \quad Q = UI \sin \varphi > 0$$

$$90^\circ < \varphi < 180^\circ \quad -P$$

Active Power (W)
Consumption

$$\cos \varphi_{\text{III}} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} < 0$$

$$\cos \varphi < 0 \quad P = UI \cos \varphi < 0$$

$$\sin \varphi > 0 \quad Q = UI \sin \varphi > 0$$

$$180^\circ < \varphi < 270^\circ$$

Producer Reference Frame (PRF)

Reactive Power (VAr) Feed-In

Overexcited

QUADRANT II
Battery charging

Overexcited
QUADRANT I
Battery discharging

Battery charging
QUADRANT III
Underexcited

Battery discharging
QUADRANT IV
Underexcited

Reactive Power (VAr)
Consumption

$$\cos \varphi_{\text{I}} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} > 0$$

$$\cos \varphi > 0 \quad P = UI \cos \varphi > 0$$

$$\sin \varphi > 0 \quad Q = UI \sin \varphi > 0$$

$$0 < \varphi < 90^\circ$$

Active Power (W)
Feed-In

$$\cos \varphi_{\text{IV}} = \frac{P}{S} = \frac{P}{\sqrt{P^2 + Q^2}} > 0$$

$$\cos \varphi > 0 \quad P = UI \cos \varphi > 0$$

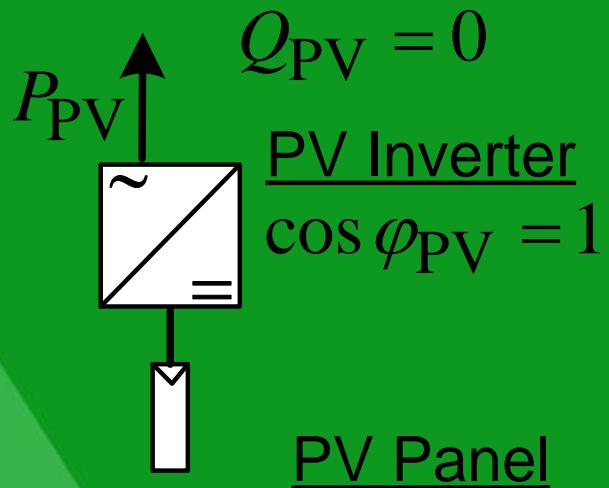
$$\sin \varphi < 0 \quad Q = UI \sin \varphi < 0$$

$$270^\circ < \varphi < 360^\circ$$

COMPARASION TWO PV INVERTORS ON ONE PV SOURCE WITH SAME CHATACTERSTICS

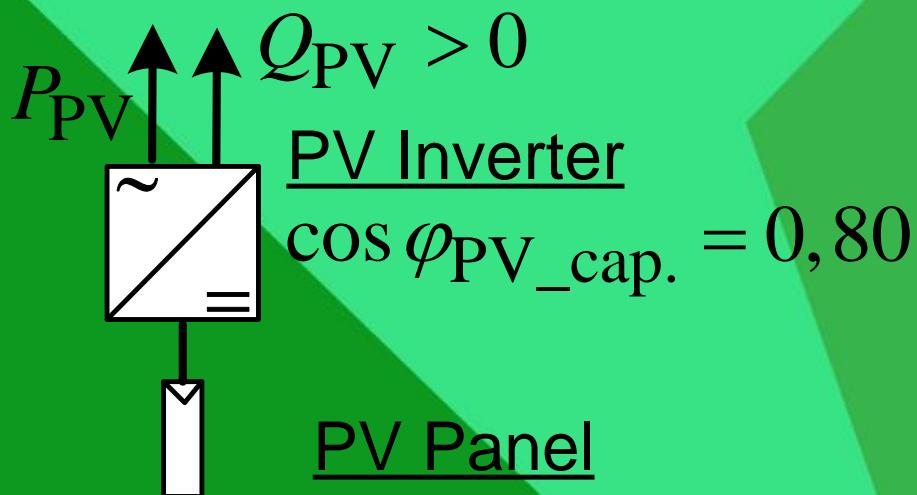
EXAMPLE 1

OLD PV INVERTER



EXAMPLE 2

PV SMART INVERTER



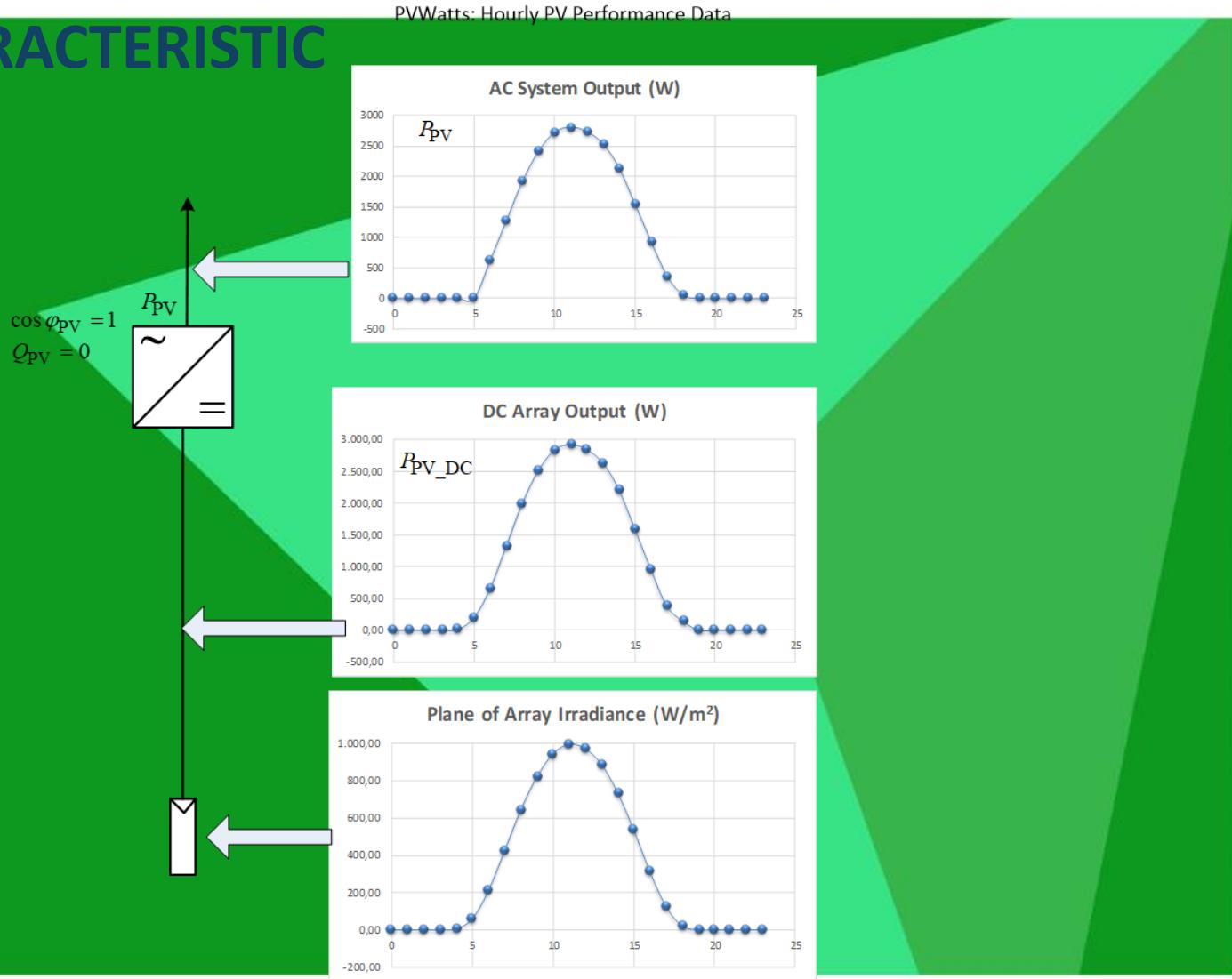


EXAMPLE 1 AND 2 - PV SOURCE CHARACTERISTIC

Daily diagram of POWER generation

SAME DATA FOR EXAMPLE 1 AND 2

PVWatts: Hourly PV Performance Data	
Requested Location:	44.708, 20.455
Location:	BELGRADE, SERBIA
Lat (deg N):	44.82
Long (deg E):	20.28
Elev (m):	99
DC System Size (kW):	4
Module Type:	Standard
Array Type:	Fixed (open rack)
Array Tilt (deg):	20
Array Azimuth (deg):	180
System Losses:	14.08
Invert Efficiency:	96
DC to AC Size Ratio:	1.2



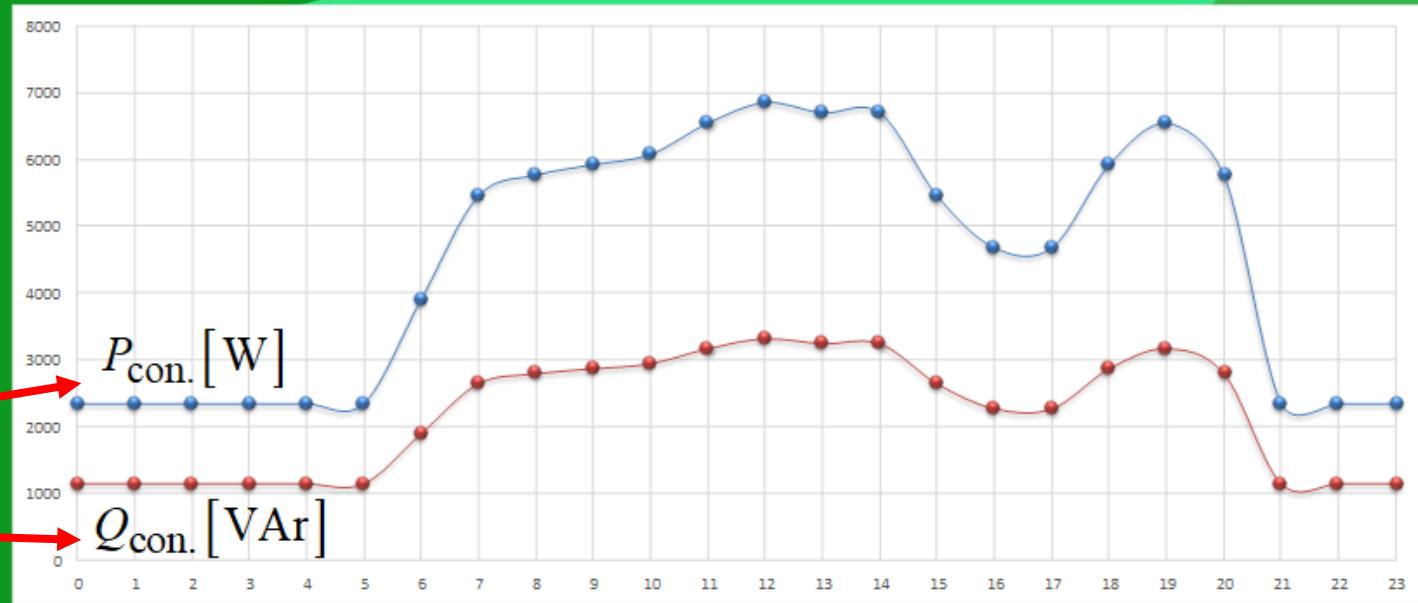
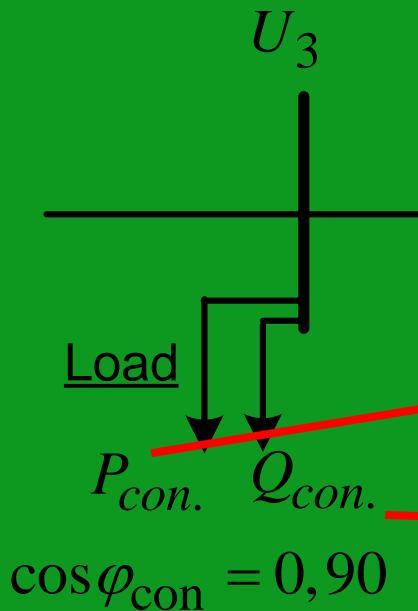
Month	Day
8	1





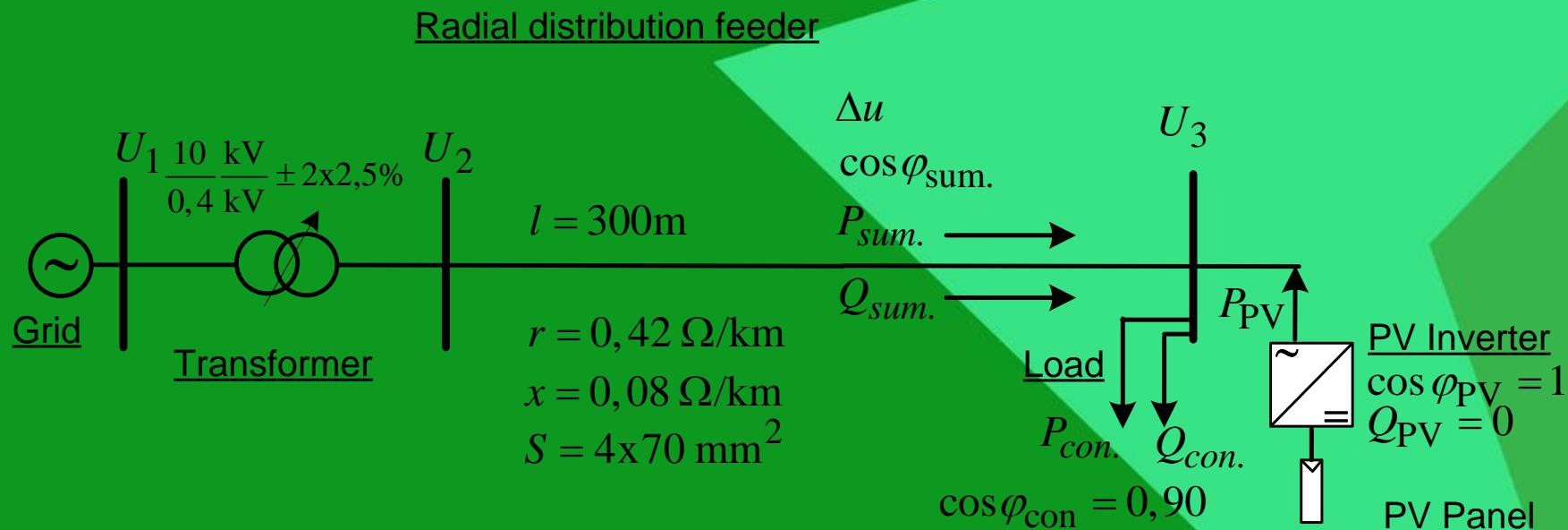
EXAMPLE 1 AND 2 – Daily diagram of POWER consumption

SAME DATA FOR EXAMPLE 1 AND 2



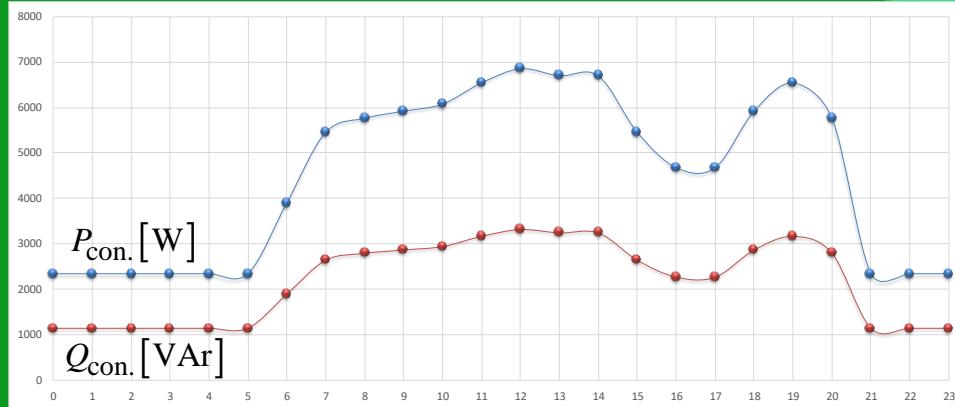


EXAMPLE 1 - RADIAL DISTRIBUTION FIDER PV INVERTER (OLD INVERTER) WITH POWER FACTOR 1

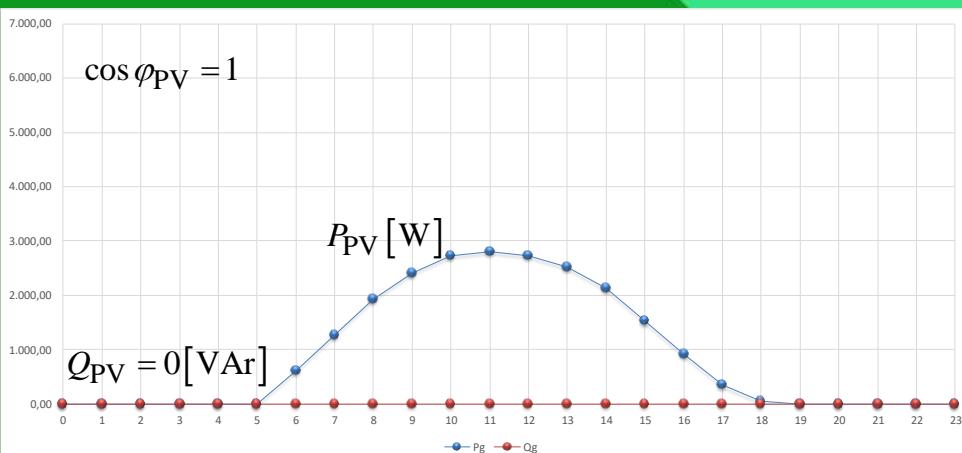




EXAMPLE 1 - RADIAL DISTRIBUTION FIDER PV INVERTER (OLD INVERTER) WITH POWER FACTOR 1



Daily diagram of
power consumption



Daily diagram of
power generation

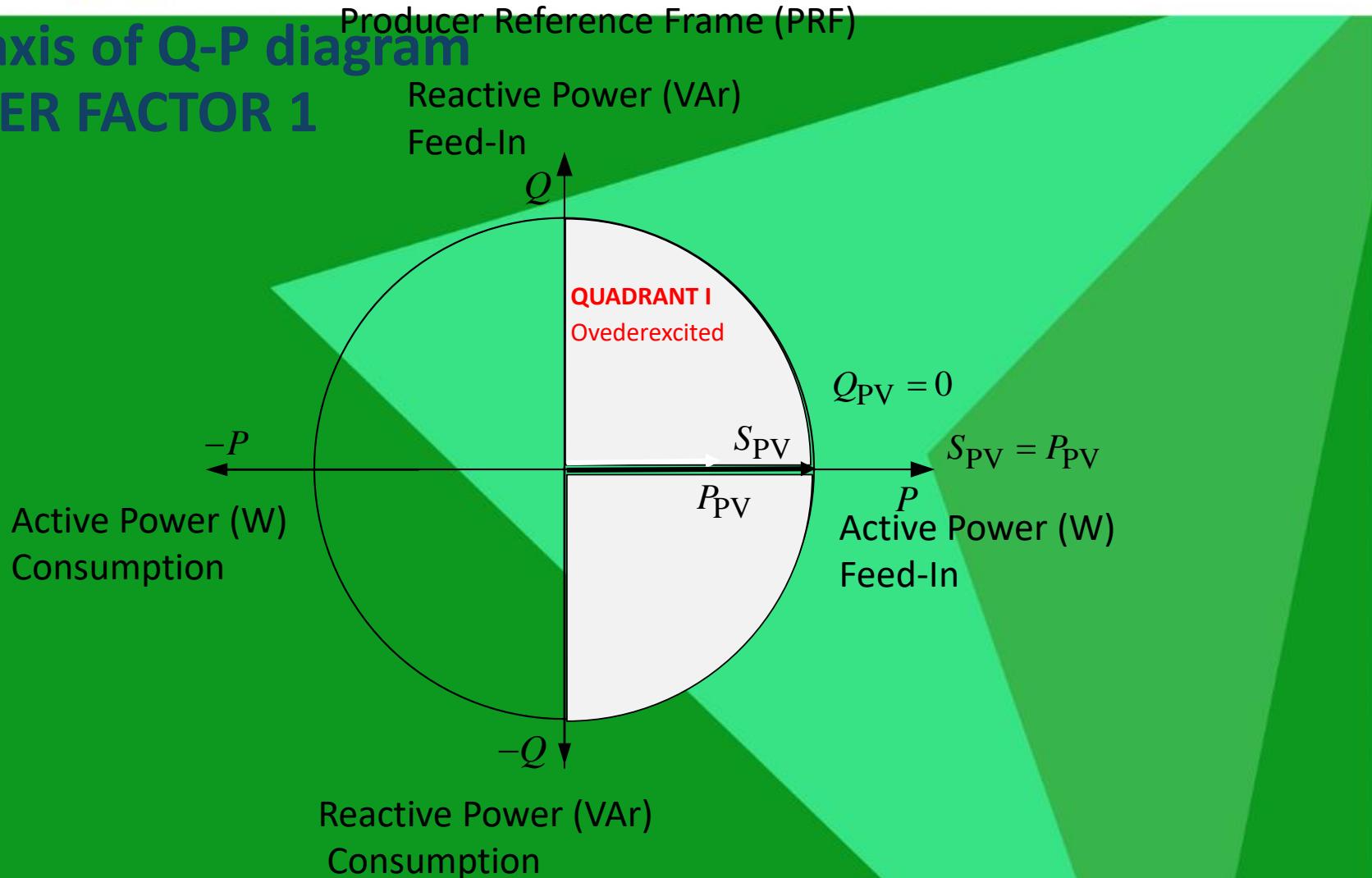
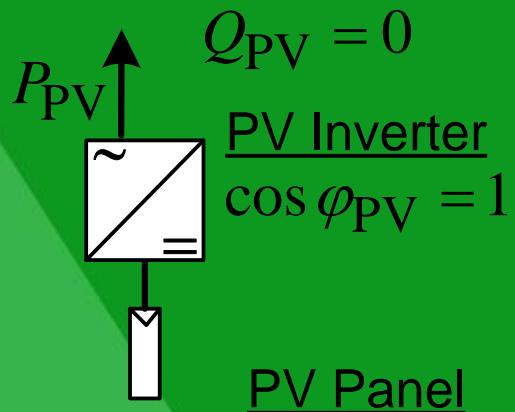


EXAMPLE 1 – work area – p axis of Q-P diagram

PV old INVERTER WITH POWER FACTOR 1

EXAMPLE 1

OLD PV INVERTER

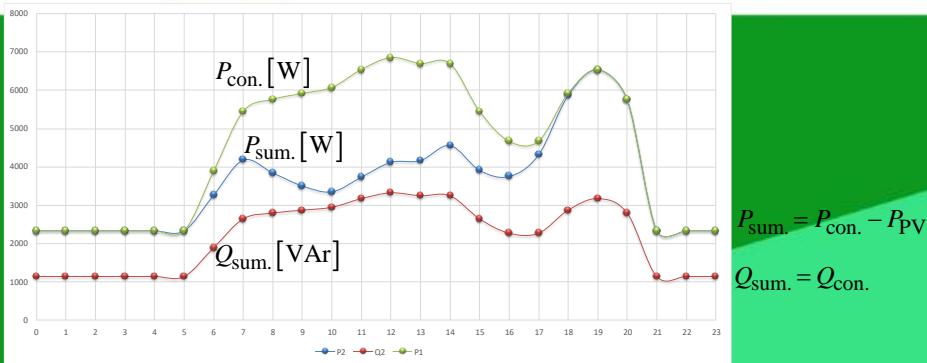




EXAMPLE 1 - RADIAL DISTRIBUTION FIDER PV INVERTER (OLD INVERTER) WITH POWER FACTOR 1

The voltage drop is smaller due to less total active power consumption on the bus 3.

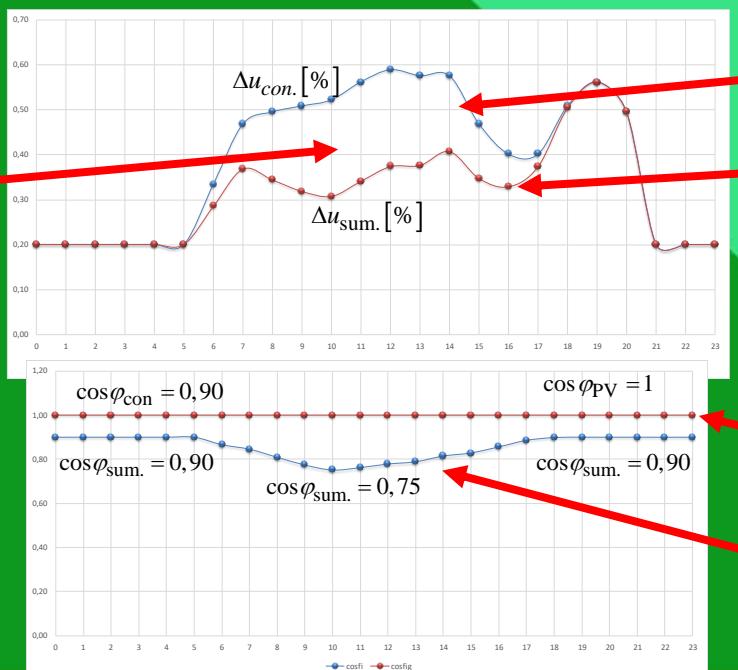
Consumer power factor decreases during the production of active power from the PV generator.



Daily diagram of active power consumption

Summary Daily diagram of active power consumption

Summary Daily diagram of reactive power consumption



Voltage drop – without PV Inverter

Voltage drop – with PV Inverter

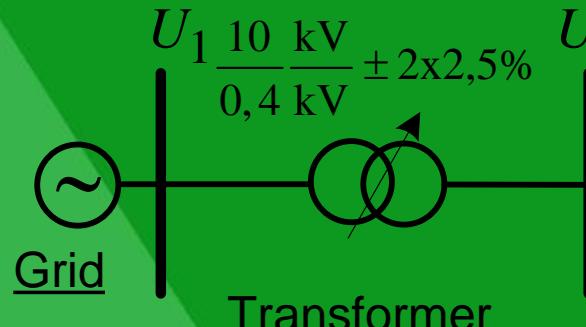
Power factor of load (0,9)

Summary Power factor of load



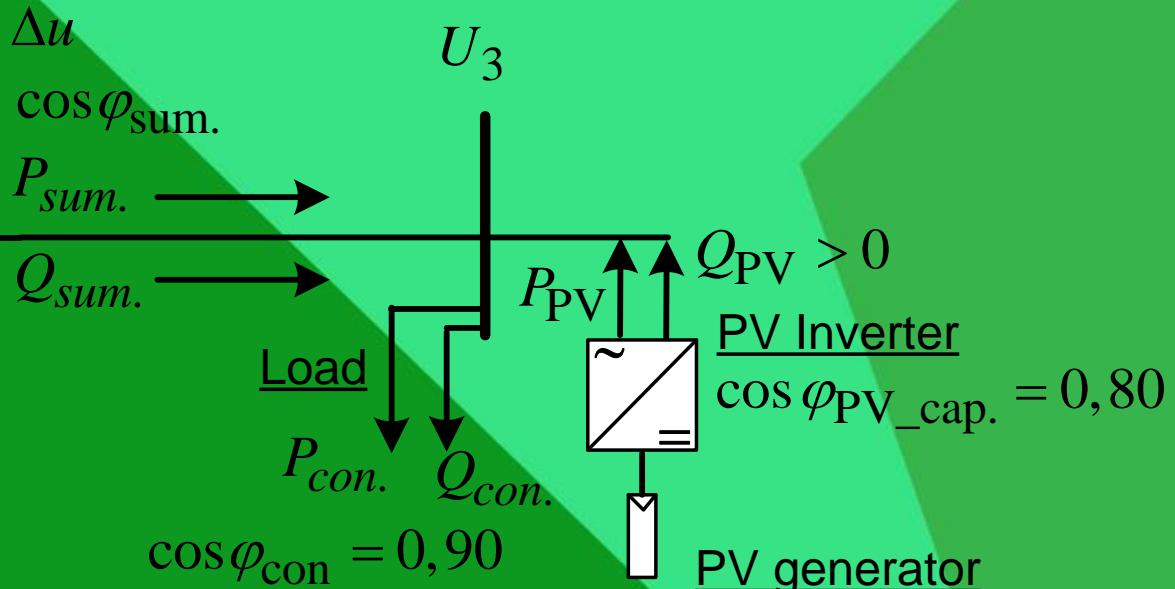
EXAMPLE 2 - RADIAL DISTRIBUTION FIDER PV SMART INVERTER WITH CONTROLABLE POWER FACTOR

Radial distribution feeder



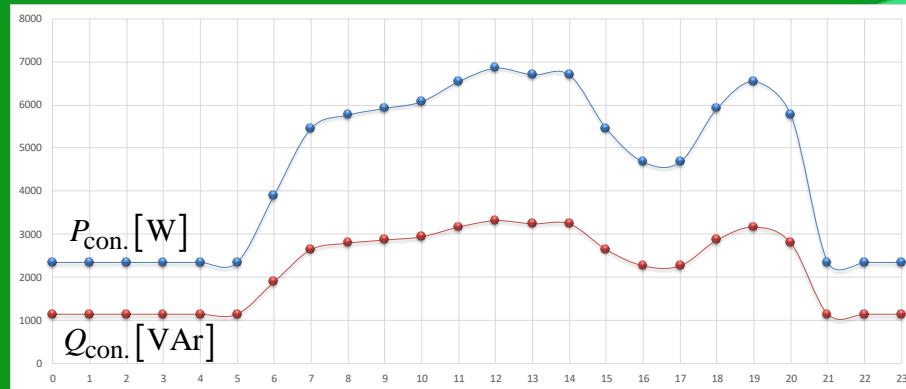
$l = 300 \text{ m}$

$$\begin{aligned} r &= 0,42 \Omega/\text{km} \\ x &= 0,08 \Omega/\text{km} \\ S &= 4 \times 70 \text{ mm}^2 \end{aligned}$$

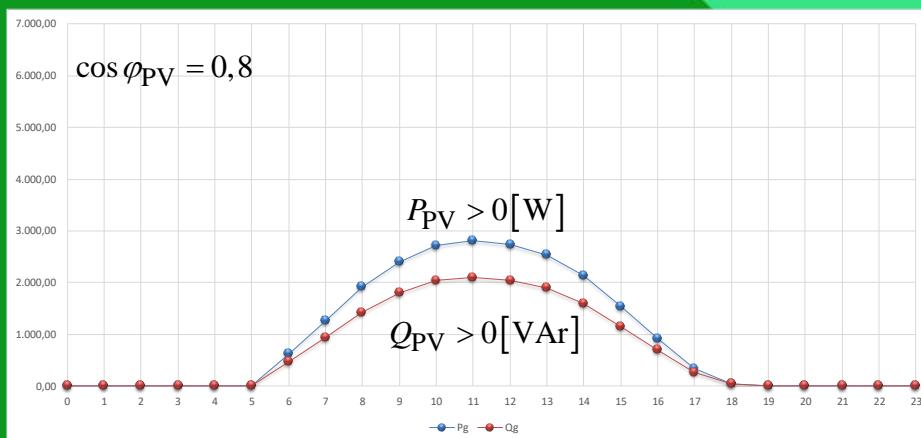




EXAMPLE 2 - RADIAL DISTRIBUTION FIDER PV SMART INVERTER WITH CONTROLABLE POWER FACTOR



Daily diagram of
power consumption



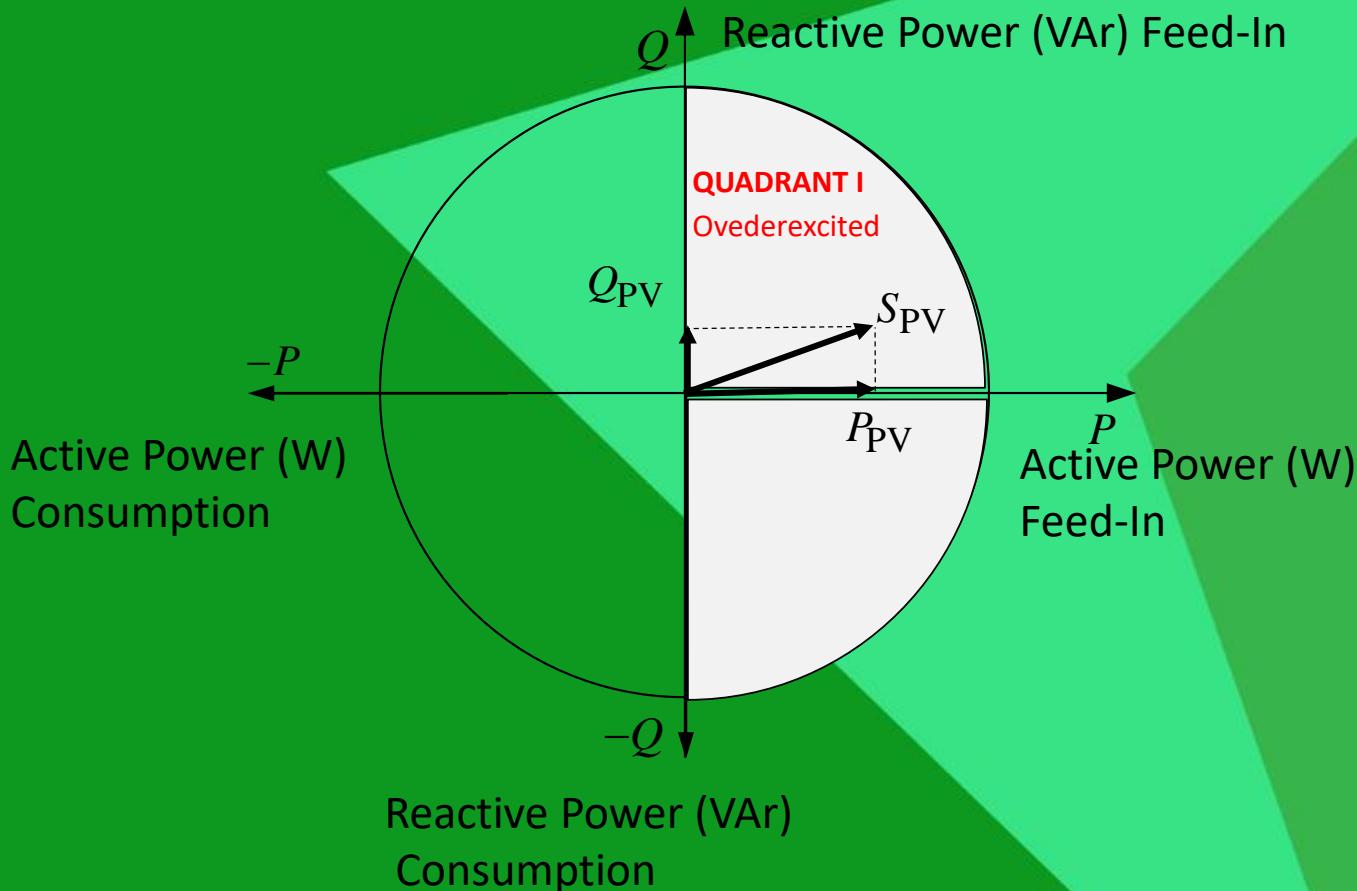
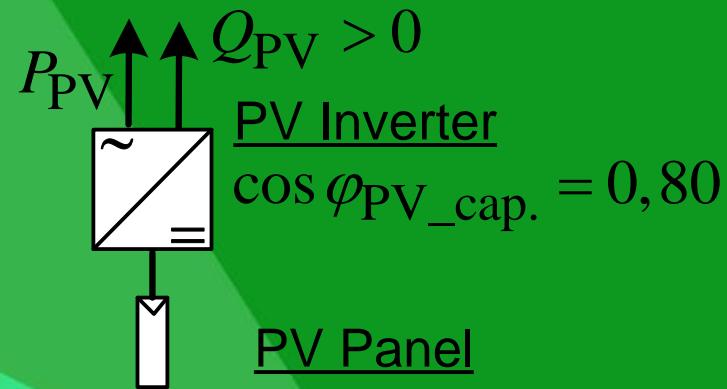
Daily diagram of
power generation



EXAPMLE 2 – work area – quadrant 1 PV SMART INVERTER WITH CONTROLABLE POWER FACTOR

Producer Reference Frame (PRF)

EXAMPLE 2 PV SMART INVERTER



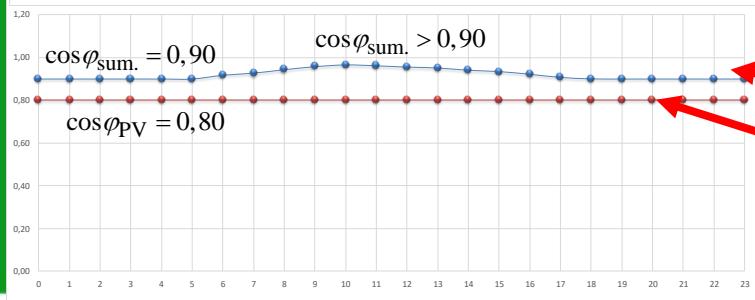
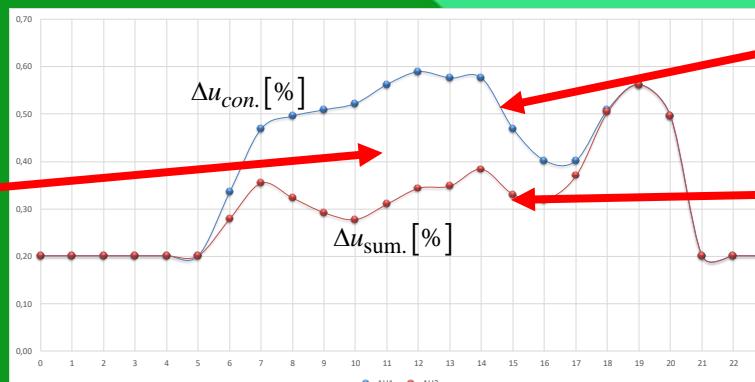
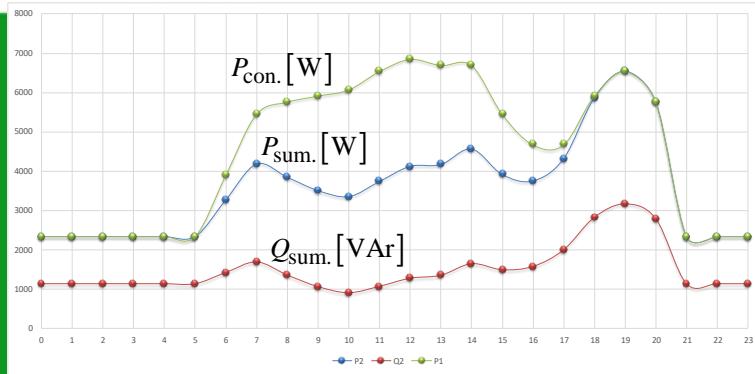


EXAPMLE 2 - RADIAL DISTRIBUTION FIDER PV SMART INVERTER WITH CONTROLABLE POWER FACTOR

The voltage drop
is smaller due to
less total active
and reactive
power
consumption on
the bus 3.

Consumer power factor
increases during the
production of active and
reactive power from the

PV generator.



Daily diagram of active power consumption

$P_{sum.} = P_{con.} - P_{PV}$
Summary Daily diagram of active power consumption

$Q_{sum.} = Q_{con.}$
Summary Daily diagram of reactive power consumption

Voltage drop – without PV Inverter

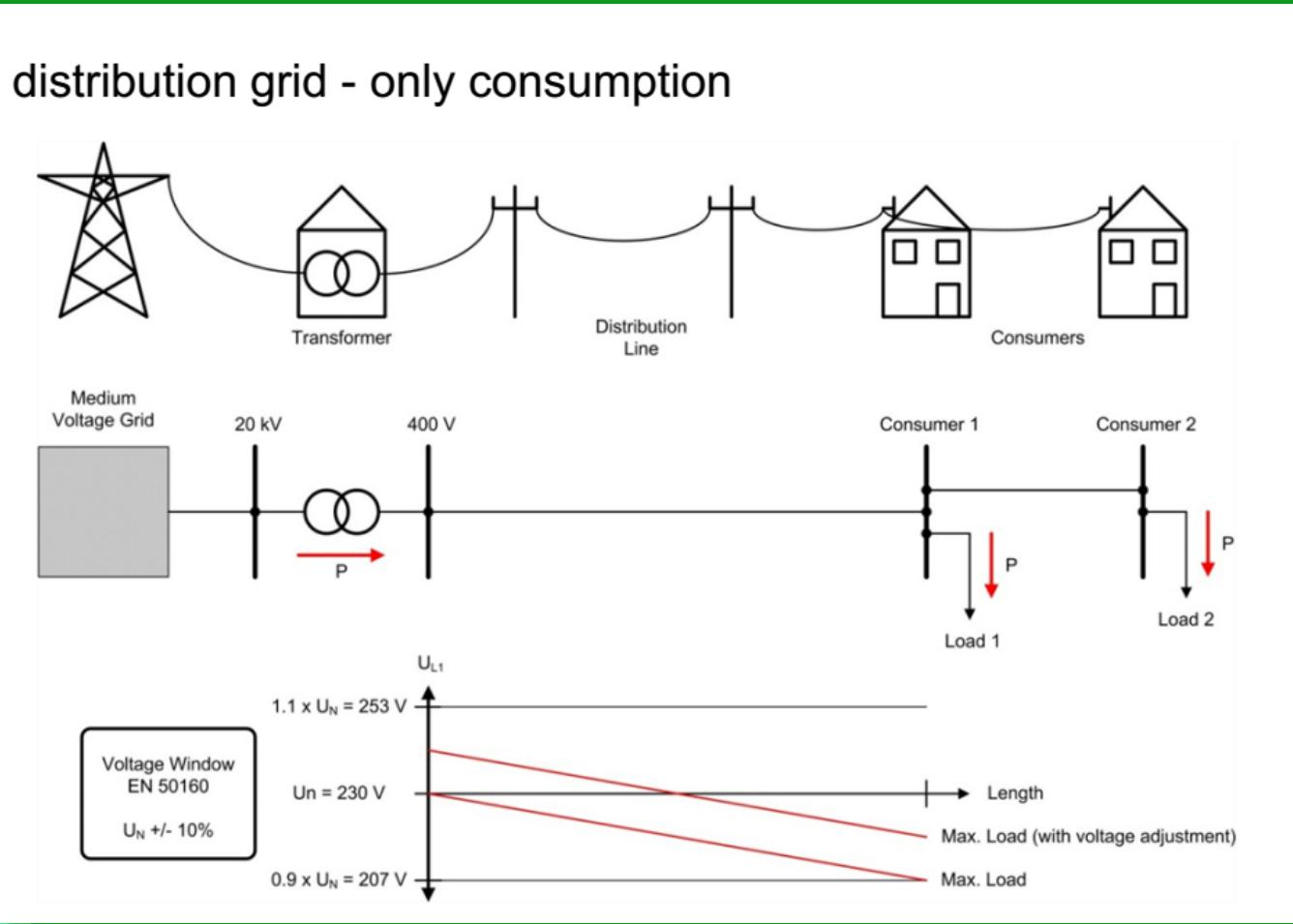
Voltage drop – with PV Inverter

Summary Power factor of load

Power factor of
PV Smart Inverter (0,8)

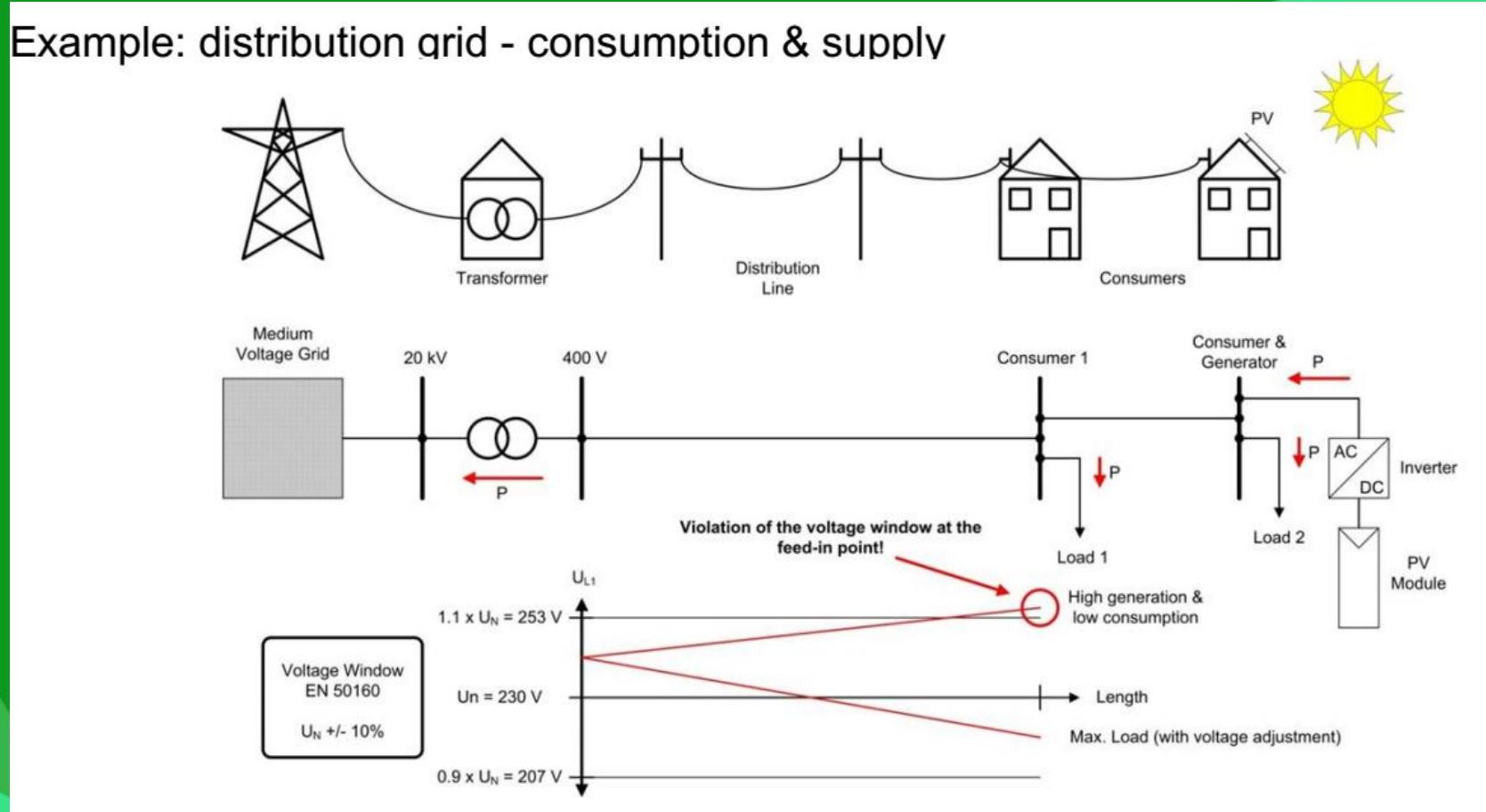


Example: distribution grid - only consumption





Example: distribution grid - consumption & supply





Distribution grid - consumption & supply incl. reactive power

